FOR EDEXCEL

GCE Examinations

Advanced Subsidiary

Core Mathematics C3

Paper F

Time: 1 hour 30 minutes

Instructions and Information

Candidates may use any calculator EXCEPT those with the facility for symbolic algebra, differentiation and / or integration.

Full marks may be obtained for answers to ALL questions.

Mathematical formulae and statistical tables are available.

This paper has eight questions.

Advice to Candidates

You must show sufficient working to make your methods clear to an examiner. Answers without working may gain no credit.



Written by Shaun Armstrong

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1. Solve the equation

$$3 \operatorname{cosec} \theta^\circ + 8 \cos \theta^\circ = 0$$

for θ in the interval $0 \leq \theta \leq 180$, giving your answers to 1 decimal place. **(6)**

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2. The functions f and g are defined by

$$\mathrm{f} : x \to 1 - ax, \quad x \in \mathbb{R},$$

$$\mathrm{g} : x \to x^2 + 2ax + 2, \quad x \in \mathbb{R},$$

where a is a constant.

(a) Find the range of g in terms of a. **(3)**

Given that $\mathrm{gf}(3) = 7$,

(b) find the two possible values of a. **(4)**

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3. *(a)* Solve the equation

$$\ln (3x + 1) = 2$$

giving your answer in terms of e. **(3)**

(b) Prove, by counter-example, that the statement

"$\ln (3x^2 + 5x + 3) \geq 0$ for all real values of x"

is false. **(5)**

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4. A curve has the equation $x = y\sqrt{1-2y}$.

(a) Show that

$$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{\sqrt{1-2y}}{1-3y}.$$ **(5)**

The point A on the curve has y-coordinate -1.

(b) Show that the equation of tangent to the curve at A can be written in the form

$$\sqrt{3}\,x + py + q = 0$$

where p and q are integers to be found. **(3)**

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5. *(a)* Sketch the graph of $y = 2 + \sec\left(x - \frac{\pi}{6}\right)$ for x in the interval $0 \leq x \leq 2\pi$.

Show on your sketch the coordinates of any turning points and the equations of any asymptotes. **(5)**

(b) Find, in terms of π, the x-coordinates of the points where the graph crosses the x-axis. **(5)**

6.

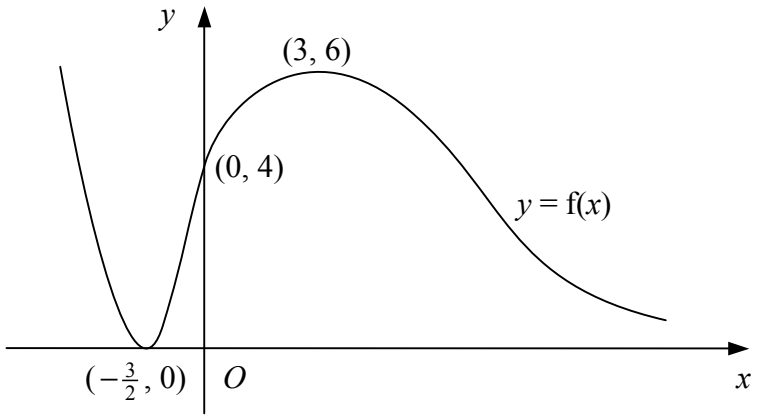


Figure 1

Figure 1 shows the curve $y = f(x)$ which has a minimum point at $(-\frac{3}{2}, 0)$, a maximum point at (3, 6) and crosses the y-axis at (0, 4).

Sketch each of the following graphs on separate diagrams. In each case, show the coordinates of any turning points and of any points where the graph meets the coordinate axes.

(a) $y = f(|x|)$ **(3)**

(b) $y = 2 + f(x + 3)$ **(4)**

(c) $y = \frac{1}{2} f(-x)$ **(4)**

Turn over

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7. $$f(x) = 1 + \frac{4x}{2x-5} - \frac{15}{2x^2-7x+5}, \quad x \in \mathbb{R}, \quad x < 1.$$

(a) Show that

$$f(x) = \frac{3x+2}{x-1}.$$ **(5)**

(b) Find an expression for the inverse function $f^{-1}(x)$ and state its domain. **(5)**

(c) Solve the equation $f(x) = 2$. **(2)**

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8. A curve has the equation $y = x^2 - \sqrt{4+\ln x}$.

(a) Show that the tangent to the curve at the point where $x = 1$ has the equation

$$7x - 4y = 11.$$ **(5)**

The curve has a stationary point with x-coordinate α.

(b) Show that $0.3 < \alpha < 0.4$ **(3)**

(c) Show that α is a solution of the equation

$$x = \tfrac{1}{2}(4 + \ln x)^{-\frac{1}{4}}.$$ **(2)**

(d) Use the iteration formula

$$x_{n+1} = \tfrac{1}{2}(4 + \ln x_n)^{-\frac{1}{4}},$$

with $x_0 = 0.35$, to find x_1, x_2, x_3 and x_4, giving your answers to 5 decimal places. **(3)**

END

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